# **Charge Self-compensation in the Nonlinear Optical Crystals Rb0.855Ti0.955Nb0.045OPO4 and RbTi0.927Nb0.056Er0.017OPO4**

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We used X-ray single-crystal diffraction (XRD) and high-resolution neutron powder diffraction (NPD) and performed second-harmonic generation (SHG) measurements to investigate the structural details and nonlinear optical (NLO) properties of  $Rb_{0.855}Ti_{0.955}$ - $Nb_{0.045}OPO_4$  and  $RbTi_{0.927}Nb_{0.056}Er_{0.017}OPO_4$ . We studied in detail the distribution of Nb<sup>5+</sup> and  $Er<sup>3+</sup>$  doping cations among the different types of TiO<sub>6</sub> octahedra in the structure. We found that Nb cations exclusively occupied Ti(1) sites, but we did not observe a preferential occupation of the octahedra by Er. Our results established that, in  $Rb_{0.855}Ti_{0.955}Nb_{0.045}OPO<sub>4</sub>$ , the substitution of  $Ti^{4+}$  by Nb<sup>5+</sup> centers was compensated by the creation of Rb<sup>+</sup> vacancies. The SHG measurements in these crystals reveal that these crystals are excellent nonlinear optical materials and that the absorption of the generated green light by  $Er^{3+}$  in the RbTi<sub>0.927</sub>- $Nb_{0.056}Er_{0.017}OPO_4$  crystal is negligible.

## **Introduction**

Potassium titanyl phosphate,  $KTiOPO<sub>4</sub>$  (KTP), is the best-known member of the family of compounds with formula  $MM'OXO<sub>4</sub>$  (M = K, Rb, Tl, Na, NH<sub>4</sub> or Cs; M'  $=$  Ti, Ge, Sn; and  $X = P$  or As; or partial substitution in M and M' by two or more different cations).<sup>1,2</sup> Many of the crystals in this family are interesting because of their nonlinear optical (NLO) properties. KTP is particularly interesting for its application in the secondharmonic generation of 1.064-μm Nd lasers.<sup>3</sup> All members of this family are orthorhombic, biaxial crystals and belong to the noncentrosymmetric space group *Pna*21 (point group *mm*2). The structure is characterized by helicoidal chains of  $M'O_6$  octahedra that are linked between them at two corners and separated by  $XO<sub>4</sub>$ tetrahedra.4

Many isostructural analogues have been synthesized.<sup>5</sup> This family of compounds is therefore particularly good for investigating the relationship between crystal structure and optical properties. Several isomorphous substitutions have been made in the KTP structure to

determine the origin of its NLO properties. A few substitutions have maintained or improved the secondharmonic generation (SHG) response of KTP.<sup>6</sup> The main reason for this seems to be the deformation of the  $M'O_6$ octahedra: the more distorted these octahedral are, the higher the efficiency of SHG of the material.<sup>7,8</sup>

Niobium is known to substitute isomorphously for Ti in a number of mixed-titanate compounds such as KTP:Nb $^6$  or K(TiNb)O5. $^9$  This last family of compounds, with a different structure from that of KTP, can be made nonstoichiometric with a chemical formula of the type  $K_{1-x}(Ti_{1-x}Nb_{1+x})O_5$ <sup>10</sup> In both structures, the presence of Nb is compensated by vacancies in the K site. In the case of  $Nb<sup>5+</sup>$ , many different types of charge compensators were reported with the KTP structure: first, on the octahedral site by  $Ga^{3+}$  with a partial charge compensation and  $K^+$  vacancies induced<sup>11</sup> and Mg<sup>2+</sup> in K(Ti<sub>1-*x*</sub>(Mg<sub>1/3</sub>Nb<sub>2/3</sub>)<sub>*x*</sub>)OPO<sub>4</sub> without induction of  $K^+$  vacancies;<sup>12</sup> second, on the tetrahedral site, by  $\mathrm{Si}^{4+}$ with the structure  $K_{1.16}(Ti_{0.37}Nb_{0.63})(Si_{0.63}P_{0.53})O_{5.48}.^{13}$ Also,  $Ti^{4+}$  cations in KTiOAsO<sup>4</sup> (KTA) crystals can be completely substituted with  $(Nb^{5+}-M^{3+})^{14}$  cation pairs

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(with  $M = Al$ , Cr, Ga, Fe, In) on the octahedral site and<br>it seems to be that  $Ti^{4+}$  can be completely substituted by  $Nb^{5+}$  when  $Ge^{4+}$  substituted As in the tetrahedral site in KTA crystals.14 It was demonstrated that the KTA matrix was more stable for this substitution than the KTP matrix because the corresponding  $K(Nb^{5+},M^{3+})$ - $OPO<sub>4</sub>$  phase was not observed. Cheng et al.<sup>15</sup> reported that substituting the Ti<sup>4+</sup>-K<sup>+</sup> pair with Nb<sup>5+</sup> in the KTP crystal increases the optical birefringence and makes the material suitable for the SHG of blue light. Wei et al.<sup>16</sup> reported noncritical phase matching from YAG:Nd 1.06-*µ*m laser in 4.0% KTP:Nb crystal and obtained 4% efficiency in their first experiment. Our study deals with the preparation of solid solution crystals of the  $RbTiOPO<sub>4</sub>$  family, obtained from the substitution of Ti<sup>4+</sup> with  $(Nb^{5+}-\tilde{L}n^{3+})$ .

Doping these crystals with lanthanide  $(Ln^{3+})$  ions is interesting because the ion photoluminescence and the NLO properties of the matrix can be merged to achieve self-induced effects. In previous studies,  $17-19$  we showed that when we used RTP crystals doped with Nb as a matrix to host  $Ln^{3+}$ , an  $Er^{3+}$  concentration similar to that obtained in other laser matrixes was achieved.  $Er^{3+}$ is interesting because of its emission around 1.5  $\mu$ m.<sup>20</sup> This ion is used in optical communications at long distances because of its efficient emission near the region of losses in silica fibers.<sup>21</sup> It is also used in medicine because of its emission at around 2.8  $\mu$ m.<sup>22</sup>

In this study, we have refined the structure of two new crystals: Rb<sub>0.855</sub>Ti<sub>0.955</sub>Nb<sub>0.045</sub>OPO<sub>4</sub> and RbTi<sub>0.927</sub>-Nb0.056Er0.017OPO4. We paid particular attention to the positions occupied by dopant cations Nb and Er in the structure and measured the SHG efficiency in both materials. Finally, we compared our results with those of other members of this family and their respective NLO properties.

# **Experimental Procedures**

**Crystal Growth.** RbTiOPO4 doped with Nb (RTP:Nb) and co-doped with Nb and Er (RTP:(Nb,Er)) were obtained from solutions of molar composition  $Rb_2O-P_2O_5-TiO_2-Nb_2O_5 Er_2O_3 = 42.9 - 35.1 - 19.8 - 2.2 - 0$  and  $42.0 - 28.0 - 27.6 - 1.5$ 0.9, respectively, by spontaneous nucleation on a Pt wire. The experiments were carried out in a vertical tubular furnace controlled by a Eurotherm 818P controller/programmer using  $25$ -cm<sup>3</sup> platinum crucibles filled with about 15 g of solution.  $Rb_2CO_3$ , NH<sub>4</sub>H<sub>2</sub>PO<sub>4</sub>, TiO<sub>2</sub>, Nb<sub>2</sub>O<sub>5</sub>, and Er<sub>2</sub>O<sub>3</sub> (p.a.) were used as initial reagents, mixed in the desired ratios, and heated until bubbling of  $NH_3$ ,  $H_2O$ , and  $CO_2$  was complete. The solution was homogenized by maintaining the temperature at

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about 50-100 K above the expected saturation temperature for 3-5 h, 1190 and 1180 K being the saturation temperatures of RTP:Nb and RTP:(Nb,Er) crystals, respectively. The difference in temperature between the surface of the solution and the bottom of the crucible was about 15 K. The temperature of the homogeneous solution was lowered in 10 K steps every 30 min, until crystals appeared on the platinum wire immersed in the solution. Then, we replaced the platinum wire with a platinum disk in contact with the surface of the solution to obtain larger crystals. After that, the temperature was decreased 20 K at a rate of 2.5 K/h to obtain the crystals with good enough quality and quantity for the latter characterizations. The quality of the crystallized phases was first checked by laboratory X-ray powder diffraction using a Siemens D5000 powder diffractometer.

**Dopant Concentration Analyses.** The crystals obtained were cleaned and analyzed by electron probe microanalysis (EPMA) to determine the concentration of the doping elements. A CAMECA SX-50 operating in wavelength dispersive mode was used. The samples were included in a polyester ortoftalictype resin and the surfaces of the samples were polished using diamond powders until a grain size of 1 *µ*m was reached. The concentrations of Rb, Ti, P, Nb, and O were analyzed at an electron current of 30 nA and the concentration of Er was analyzed at 100 nA. In all cases, the accelerating voltage was maintained at 25 kV. The raw intensities were corrected for dead time, background, and matrix effects using the PAP correction procedure.23 The error in the determination of the content of Rb, Ti, and P in the samples in weight percent were around 1%, for Nb and O were around 3%, and for Er was around 15%. The cation concentrations from these analyses were taken as the nominal compositions in the two types of crystals of this work.

**Single-Crystal X-ray Diffraction.** A small piece of an asgrown crystal of RTP:Nb was selected (to avoid defects that are easily introduced in the material by cutting and polishing) to determine its single-crystal X-ray structure (XRD). Singlecrystal XRD measurements were carried out at RT, and the structure was resolved by Patterson synthesis. Details of crystal data, data collection, and refinement are given in Table 1.

**Neutron Powder Diffraction.** Neutron powder diffraction (NPD) measurements on RTP:(Nb,Er) were taken with the D2B high-resolution diffractometer at the Institut Laue Langevin (Grenoble, France). This diffractometer is equipped with a bank of 64 detectors separated by 2.5° 2*θ*, spanning an angular range of 160°. A good quality pattern was obtained at room temperature (RT) in the high-flux mode of D2B (see Figure 1). The wavelength used was 1.594 Å and the counting time was run about 3 h to have the desired statistics over the angular range 0-160° 2*θ*. NPD data were analyzed by the Rietveld method, using the refinement program FULLPROF.24

**Second-Harmonic Generation.** The SHG properties of these crystals were studied by a powder technique.<sup>25</sup> The samples, powdered and graded between 5 and 20 *µ*m by standard sieves, were loaded into a 2-mm-thick quartz cell using a vibrator to ensure uniform packing. The powder was illuminated with a YAG:Nd pulsed laser. We estimated the fundamental power by measuring the 1064-nm energy reflected by the sample. The back-scattered harmonic power generated by the sample was collected using a lens and focused on a Si detector. We analyzed intersignals using a digital oscilloscope and used the ratio between the two maxima to describe the SHG efficiency process. This ratio was averaged over 100 laser shots. With this method we cannot measure the absolute efficiency of the SHG of the samples, so we compared this ratio with that of pure KTP, whose SHG efficiency is well-established in the literature.<sup>26</sup>

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Table 1. Crystal Data, Data Collection, and Refinement of Rb<sub>0.855</sub>Ti<sub>0.955</sub>Nb<sub>0.045</sub>OPO<sub>4</sub> by X-ray Single-Crystal Diffraction

	Crystal Data	
$Rb_{0.855}Ti_{0.955}Nb_{0.045}OPO_4$		Mo $K\alpha$ radiation
formula weight $= 233.81$		$\lambda = 0.71069 \text{ Å}$
orthorhombic		cell parameters from 25 reflections
Pna2 <sub>1</sub>		$\theta = 12-21^{\circ}$
$a = 12.947(3)$ Å		$\mu = 11.495$ mm <sup>-1</sup>
$b = 6.498(3)$ Å		
$c = 10.579(7)$ Å		
$\alpha = \beta = \gamma = 90^{\circ}$		$T = 293(2)$ K
		equidimensional
		0.2-mm diameter
$V = 890.0(7)$ Å <sup>3</sup>		colorless
$Z=8$		
$D_x = 3.490$ Mg m <sup>-3</sup> $D_m$ = (not measured)		
	Data Collection	
<b>Enraf-Nonius CAD-4</b>		$R_{\rm int} = 0.035$
$\omega/2\theta$ scan		$\theta_{\rm max} = 29.95^{\circ}$
absorption correction: $\varphi$ -scan		$h = 0-18$
1382 measured reflections		$k = 0-9$
1360 independent reflections		$l = 0 - 14$
1114 reflections with $I > 2\sigma(I)$		
	Refinement	
refinement on $F^2 R[F^2 > 2\sigma(F^2)] = 0.0328$		$\Delta \rho_{\text{max}}$ = 0.646 e Å <sup>-3</sup>
$wR(F^2) = 0.0788$		$\Delta \rho_{\rm min} = -0.354$ e Å <sup>-3</sup>
$S = 1.019$		
1360 reflections		
148 parameters		Flack absolute structure parameter
$W = 1/[\sigma^2(F_0^2) + (0.0469P)^2]$		scattering factors from Internation
where $P = (F^2 + 2F^2)/3$		for Crystallography (yol C)

### **Results**

where  $P = (F_0^2 + 2F_c^2)/3$ 

**Structural Characterization.** The crystals obtained had the characteristic shape of RTP crystals. There was only one difference: doping with niobium flattened them somewhat, as we explained in detail in a previous study.17 The as-grown crystals were light gray-bluish, but this color disappeared after an additional 3 h of annealing of the crystal in air at 773 K. In crystals containing Er, the characteristic pale pink color of this ion remained, while RTP:Nb crystals were colorless or pale yellow. The samples were free of impurities and the structural refinements of single-crystal XRD and NPD data were performed in the orthorhombic *Pna*21 space group.

*Rb0.855Ti0.955Nb0.045OPO4 Structure.* We solved the structure of  $Rb_{0.855}Ti_{0.955}Nb_{0.045}OPO<sub>4</sub>.$  The unit cell parameters were  $a = 12.947(3)$  Å,  $b = 6.498(3)$  Å, and  $c = 10.579(7)$  Å and  $Z = 8$ . Parameter *a* was shorter, *b* was slightly longer, and *c* was clearly longer than the corresponding ones in the RTP structure. Details of crystal data, refinement, and atomic coordinates are given in Tables 1 and 2.

The main characteristic of this structure is that we obtained the enantiomorphic image of pure RTP. This means that while the *x* and *y* coordinates for all the atoms did not change very much, the *z* coordinates shifted considerably and were related to the *z* coordinate of pure RTP structure with a mirror plan at a height of practically a quarter in the *c* direction. This feature was also observed in the KTP:Nb structure when it was compared to that of pure KTP.6,27

Table 3 shows the occupation factors of the  $Rb_{0.855}$ - $Ti_{0.955}Nb_{0.045}OPO_4$  structure. The occupancies of the crystallographically independent positions for rubidium

ck absolute structure parameter  $= -0.027(14)$ scattering factors from *International Tables for Crystallography* (vol. C)

cations were  $0.832(5)$  for Rb(1) and  $0.878(5)$  for Rb(2). This follows the same trend as in the KTP:Nb samples.<sup>27</sup> The occupancies of Ti sites were 0.910(8) and 0.090(8) for Ti and Nb, respectively, in Ti(1) positions and 1.000- (8) and 0.000(8) for the same cations in Ti(2) positions. We refined the Ti occupancies by assuming that each of these positions were fully occupied by titanium and niobium atoms. There is a tendency for Nb to occupy only the Ti(1) position.

The anisotropic displacements parameters of the atoms are given in Table 4.

*RbTi0.927Nb0.056Er0.017OPO4 Structure.* We used the structure of Rb<sub>0.855</sub>Ti<sub>0.955</sub>Nb<sub>0.045</sub>OPO<sub>4</sub> as a starting model to refine the structure of the  $RbTi_{0.927}Nb_{0.056}Er_{0.017}OPO_4$ crystal by NPD. By carefully analyzing high-resolution NPD data, we were able to study fine structural details such as oxygen positions and, in particular, to determine the location of dopants. In the refinements we used a pseudo-Voigt profile function corrected for asymmetry and a six-parameter polynomial function to reproduce the background.

Table 5 shows the RT cell parameters, refined atomic coordinates, and isotropic temperature factors of  $RbTi<sub>0.927</sub>$  $Nb_{0.056}Er_{0.017}OPO_4$  structure from NPD. It also shows the final reliability factors. Figure 1 illustrates the agreement between the observed and calculated NPD profiles. The high-angle region of the refined NPD pattern (see Figure 1b) illustrates the excellent agreement between the observed and calculated NPD profiles for the best fit, which provide the occupations shown in Table 3.

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Figure 1. (a) Refined neutron diffraction pattern of RbTi<sub>0.927</sub>- $Nb_{0.056}Er_{0.017}OPO_4$  showing the observed (points), calculated (full line), and difference (bottom) Rietveld profiles at RT (D2B data). (b) Detail of the high-angle region of the refined neutron diffraction pattern.

**Table 2. Atomic Coordinates and Equivalent Isotropic** Displacement Parameters of  $Rb_{0.855}Ti_{0.955}Nb_{0.045}OPO<sub>4</sub>$ **from X-ray Single-Crystal Diffraction**

		<b>Cell Parameters</b>		
$a(A) =$		$b(A) =$	$c(A) =$	$V(\AA^3) =$
12.947(3)		6.498(3)	10.579(7)	890.0(7)
atom	$\boldsymbol{X}$	У	Z	$U$ (eq)
Ti(1)	0.3726(1)	0.5001(1)	0.4438(1)	0.021(1)
Nb(1)	0.3726(1)	0.5001(1)	0.4438(2)	0.021(1)
Ti(2)	0.2485(1)	0.2660(2)	0.6950(1)	0.018(1)
P(1)	0.4997(2)	0.3350(2)	0.7001(2)	0.038(1)
P(2)	0.1810(1)	0.5015(3)	0.9530(2)	0.050(1)
Rb(1)	0.3862(1)	0.7852(2)	0.7666(1)	0.042(1)
Rb(2)	0.1045(1)	0.6896(2)	0.5173(1)	0.039(1)
O(1)	0.4882(4)	0.4773(10)	0.5878(6)	0.041(1)
O(2)	0.5129(5)	0.4638(11)	0.8243(5)	0.042(1)
O(3)	0.4008(5)	0.2070(9)	0.7182(6)	0.043(1)
O(4)	0.5945(4)	0.1909(8)	0.6756(5)	0.040(1)
O(5)	0.1124(4)	0.3128(8)	0.9829(5)	0.040(1)
O(6)	0.1128(4)	0.6928(9)	0.9275(7)	0.037(1)
O(7)	0.2510(5)	0.5466(9)	1.0688(5)	0.041(1)
O(8)	0.2516(5)	0.4615(9)	0.8416(6)	0.045(1)
OT(1)	0.2210(5)	0.9611(9)	1.0833(5)	0.043(1)
OT(2)	0.2240(5)	0.0479(10)	0.8317(5)	0.045(1)

The volume of the unit cell was larger because of the increase in the atomic radii of  $Er^{3+}$ , but the distribution of this larger volume was not the same for all three cell parameters: *a* and *b* were 0.19 and 0.14% longer, respectively, and *c* was 0.05% shorter than the param-

**Table 3. Occupation Factors at the Ti and Rb Sites in Rb0.855Ti0.955Nb0.045OPO4 and RbTi0.927Nb0.056Er0.017OPO4**

	occupation factor		
atom	$Rb_{0.855}Ti_{0.955}Nb_{0.045}OPO_4$ from X-ray single- crystal diffraction	$RbTi_{0.927}Nb_{0.056}Er_{0.017}OPO_4$ from neutron powder diffraction	
Ti(1) Nb(1) Er(1)	0.910(8) 0.090(8)	0.871(6) 0.111(6) 0.017(6)	
Ti(2) Nb(2) Er(2)	1.000(8) 0.000(8)	0.983(6) 0.000(6) 0.017(6)	
Rb(1)	0.832(5)	1.000(4)	
Rb(2)	0.878(5)	1.000(4)	

**Table 4. Anisotropic Displacement Parameters (Å2) of** Orthorhombic  $\tilde{Rb}_{0.855}T\tilde{i}_{0.955}Nb_{0.045}OPO_4$ ; Anisotropic **Displacement Factor Exponent Takes the Form**  $-2\pi^2[\mathbf{h}^2\mathbf{a}^{*2}U_{11}+\ldots+2\mathbf{h}\mathbf{k}\mathbf{a}^{*}\mathbf{b}^{*}U_{12}]$ 

atom	$U_{11}$	$U_{22}$	$U_{33}$	$U_{23}$	$U_{13}$	$U_{12}$
Ti(1)	0.022(1)	0.015(1)	0.026(1)	0.001(1)	$-0.001(1)$	0.000(1)
Nb(1)	0.022(1)	0.015(1)	0.026(1)	0.001(1)	$-0.001(1)$	0.000(1)
Ti(2)	0.018(1)	0.015(1)	0.021(1)	0.002(1)	0.000(1)	0.001(1)
P(1)	0.037(1)	0.032(1)	0.046(1)	0.001(1)	0.001(1)	0.001(1)
P(2)	0.062(1)	0.034(1)	0.056(1)	0.000(1)	0.001(1)	$-0.001(1)$
Rb(1)	0.045(1)	0.027(1)	0.054(1)	0.001(1)	0.004(1)	0.003(1)
Rb(2)	0.032(1)	0.033(1)	0.050(1)	0.002(1)	0.001(1)	0.004(1)
O(1)	0.036(2)	0.042(3)	0.048(3)	0.004(2)	0.001(2)	$-0.002(2)$
O(2)	0.024(3)	0.048(3)	0.056(3)	0.002(2)	0.003(2)	0.002(2)
O(3)	0.051(3)	0.027(3)	0.051(4)	0.001(3)	0.000(3)	0.003(2)
O(4)	0.041(2)	0.034(2)	0.046(3)	0.003(2)	0.000(2)	0.000(2)
O(5)	0.037(2)	0.041(2)	0.044(3)	$-0.001(2)$	0.000(2)	$-0.007(2)$
O(6)	0.048(3)	0.021(3)	0.042(3)	0.005(2)	$-0.008(2)$	$-0.004(3)$
O(7)	0.055(3)	0.035(3)	0.035(3)	$-0.003(2)$	$-0.003(2)$	0.001(3)
O(8)	0.045(3)	0.035(3)	0.055(3)	$-0.001(2)$	0.001(2)	$-0.001(2)$
OT(1)	0.036(3)	0.036(3)	0.060(3)	0.001(2)	0.000(2)	0.001(2)
OT(2)	0.036(3)	0.042(3)	0.054(3)	$-0.001(2)$	0.001(2)	0.001(2)

**Table 5. Cell Parameters, Refined Atomic Coordinates, and Isotropic Temperature Factors from RbTi0.927Nb0.056Er0.017OPO4 by Neutron Data at RT**



Reliability Factors

 $\chi^2 = 1.65\%$ ,  $R_p = 5.39\%$ ,  $R_{wp} = 6.82\%$ ,  $R_f$  factor = 4.74%, Bragg  $R$ -factor =  $6.20\%$ 

eters of the Rb<sub>0.855</sub>Ti<sub>0.955</sub>Nb<sub>0.045</sub>OPO<sub>4</sub> crystal. Our main aim was to obtain reliable information about the distribution of the small concentration of Er and Nb cations in the structure (we take advantage of the very different Fermi lengths for neutrons of Ti (3.37 fm) and Nb (7.054



Figure 2. View of the structure of the RTP family of crystals illustrating the connected paths formed by alternating Ti(1)O<sub>6</sub> and  $Ti(2)O_6$  octahedra. Projections parallel to (a) [010], (b) [100], and (c) [001] directions.

fm) or Er (8.03 fm). With this objective in mind, and using a random distribution of Nb and Er among Ti sites as a starting point, we performed different sets of Rietveld refinements of the NPD data for different models of the distribution of dopants. As expected, Nb and Er only went to Ti sites in the  $RbTi_{0.927}Nb_{0.056}Er_{0.017}$ -OPO4 structure. We also checked for the possibility of vacant oxygen or rubidium. All the atomic positions, including oxygen or rubidium sites, were fully occupied. This was in contrast to some vacant rubidium sites found in the RTP:Nb crystal. In our  $RbTi_{0.927}Nb_{0.056}$ -  $Er_{0.017}OPO_4$  crystal, within a resolution of ∼1%, we found that the two Rb sites were fully occupied.

When we impose that Er and Nb cations randomly substituted the two Ti sites, the reliability factors were  $R_{wp}$  = 6.88%,  $R_f$  = 4.79%, and  $R_{\text{bragg}}$  = 6.29%. However, when we allowed for an inhomogeneous distribution of the dopants, the reliability factors clearly improved. When we fitted the occupation factors, the refinements always converged to the same scenario: Nb atoms are only substituted Ti(1) atoms at the center of the Ti(1)- O6 octahedra. On the other hand, Nb cations did not

**Table 6. Selected Bond Distances in Rb0.855Ti0.955Nb0.045OPO4 (X-rays) and RbTi0.927Nb0.056Er0.017OPO4 (Neutrons)***<sup>a</sup>*

		$Rb_{0.855}Ti_{0.955}Nb_{0.045}OPO_4$ $RbTi_{0.927}Nb_{0.056}Er_{0.017}OPO_4$
$Ti(1)-O(1)$	2.123(6)	2.15(3)
$Ti(1)-O(2)^{i}$	1.963(6)	1.96(3)
$Ti(1)-O(5)$ ii	2.083(6)	2.15(4)
$Ti(1)-O(6)$ <sup>iii</sup>	2.013(6)	1.97(4)
$Ti(1)-OT(1)$ iii		
	1.926(6)	1.95(3)
$Ti(1)-OT(2)$ ii	1.751(6)	1.74(3)
$\langle Ti(1)-O \rangle$	1.977	1.99
$P(1) - O(1)$	1.516(6)	1.50(2)
$P(1) - O(2)$	1.567(6)	1.56(2)
$P(1)-O(3)$	1.539(6)	1.58(2)
$P(1)-O(4)$	1.566(5)	1.53(2)
$\langle P(1)-O\rangle$	1.547	1.54
$Rb(1)-O(1)$	3.042(6)	2.99(2)
$Rb(1)-O(2)$	2.725(7)	2.75(1)
$Rb(1)-O(3)v$	2.795(6)	
		2.75(1)
$Rb(1)-O(5)$ ii	3.006(6)	3.00(2)
$Rb(1)-O(6)$ <sup>vi</sup>	3.396(6)	3.41(2)
$Rb(1)-O(7)$ <sup>ii</sup>	3.227(6)	3.23(2)
$Rb(1)-O(8)$	2.844(6)	2.83(2)
$Rb(1)-OT(1)$ <sup>iii</sup>	3.181(6)	3.22(2)
$Rb(1)-OT(2)v$	2.792(6)	2.79(2)
$\langle Rb(1)-O \rangle$	3.000	2.99
$Ti(1)-Rb(1)$ <sup>iii</sup>	4.085(2)	
$Ti(1)-Rb(2)vi$	3.699(2)	
	$Rb_{0.855}Ti_{0.955}Nb_{0.045}OPO_4$	
		$RbTi_{0.927}Nb_{0.056}Er_{0.017}OPO_4$
$Ti(2)-O(3)$	2.023(6)	2.03(3)
$Ti(2)-O(4)$ iv	2.024(5)	2.01(2)
$Ti(2)-O(7)$ <sup>iii</sup>	1.953(6)	2.00(2)
$Ti(2)-O(8)$	2.005(6)	1.95(3)
$Ti(2)-OT(1)$ <sup>iii</sup>	1.777(6)	1.77(2)
$Ti(2)-OT(2)$	2.049(6)	2.06(2)
$\langle Ti(2)-O \rangle$	1.972	1.97
$P(2)-O(5)$	1.547(5)	1.56(2)
$P(2)-O(6)$	1.548(6)	1.55(2)
$P(2)-O(7)$	1.552(6)	1.56(2)
	1.514(6)	1.54(2)
$P(2)-O(8)$ $\langle P(2)-O\rangle$	1.540	1.55
$Rb(2)-O(1)$ <sup>vii</sup>	2.755(6)	2.74(2)
$Rb(2)-O(2)$ ii	3.107(7)	3.12(2)
$Rb(2)-O(3)$ <sup>ii</sup>	3.166(7)	3.19(2)
$Rb(2)-O(4)$ iv	2.989(5)	3.02(2)
$Rb(2)-O(5)$ viii	2.832(5)	2.82(2)
$Rb(2)-O(7)$ <sup>ii</sup>	3.029(6)	3.00(2)
$Rb(2)-O(8)$ <sup>ii</sup>	3.170(6)	3.19(2)
$Rb(2)-OT(1)$ iii	2.792(6)	2.75(2)
$Rb(2)-OT(2)ii$	3.104(6)	3.16(2)
$\langle Rb(2)-O \rangle$	2.993	2.99
$Ti(2)-Rb(1)$ <sup>ix</sup>	3.676(2)	
$Ti(2)-Rb(2)x$	3.936(3)	

*a* i:  $-x+1$ ,  $-y+1$ ,  $z-$ <sup>1</sup>/<sub>2</sub>, ii:  $-x+$ <sup>1</sup>/<sub>2</sub>,  $y+$ <sup>1</sup>/<sub>2</sub>,  $z-$ <sup>1</sup>/<sub>2</sub>, iii:  $-x$ <br>+<sup>1</sup>/<sub>2</sub>,  $y-$ <sup>1</sup>/<sub>2</sub>,  $z-$ <sup>1</sup>/<sub>2</sub>, iv:  $x-$ <sup>1</sup>/<sub>2</sub>,  $-y+$ <sup>1</sup>/<sub>2</sub>,  $z$ , v:  $x$ ,  $y+1$ ,  $z$ , vi:  $x+$  $^{1/2}$ ,  $-y + ^{3/2}$ , z vii:  $x - ^{1/2}$ ,  $-y + ^{3/2}$ , z viii:  $-x$ ,  $-y + 1$ ,  $z - ^{1/2}$ . ix:  $\overline{x}$ ,  $\overline{y}$  - 1,  $\overline{z}$ ,  $\overline{x}$ :  $\frac{1}{2}$  -  $\overline{x}$ ,  $\overline{y}$  -  $\frac{1}{2}$ ,  $\overline{z}$  +  $\frac{1}{2}$ .

substitute Ti atoms of the  $Ti(2)O_6$  octahedra. We were able to refine the occupation factors of Nb and Er freely, with the only constraints that the Ti octahedra were fully occupied and had no vacant sites and that the concentrations of these cations in the structure were those given by EPMA analyses. The occupation factors therefore converged to the values given in Table 3: in our RbTiOPO4 sample (doped with 5.6% Nb and 1.7% Er), Nb cations exclusively substituted Ti(1) sites. For Er, the refinements converged to the occupations 0.014- (6) for  $Er(1)$  and 0.020(6) for  $Er(2)$ . According to the errors, this is undistinguishable from or equivalent to Er being equally distributed between Ti(1) and Ti(2) (a fraction of 0.017 in each octahedra). However, the limit of the sensitivity of the technique is the highest for the

small concentration of Er, and the corresponding relative errors are very important.

**Second-Harmonic Generation.** SHG relative efficiency is defined as the ratio between  $η<sub>sample</sub>$  and  $η<sub>KTP</sub>$ , where  $\eta$  is the ratio between the powers measured at 532 and 1064 nm. In the studies of  $Rb_{0.855}Ti_{0.955}Nb_{0.045}$  $OPO<sub>4</sub>$  and RbTi<sub>0.927</sub>Nb<sub>0.056</sub>Er<sub>0.017</sub>OPO<sub>4</sub>, this was 1.2 and 0.7, respectively. These results are referred to KTP, now that the parameters of KTP are well-established in the literature.<sup>26</sup>

The SHG relative efficiency of  $Rb_{0.855}Ti_{0.955}Nb_{0.045}$ OPO4 was around 20% higher than that of KTP. As we showed in a previous study,<sup>17</sup> the SHG relative efficiency of RTP doped with Nb increases as the concentration of Nb increases until it reaches a maximum for a Nb concentration of around  $4-5$  at. % in the crystal. For higher concentrations of Nb, the SHG relative efficiency decreases. Our results therefore entirely agree with those of our previous studies of SHG relative efficiency in RTP:Nb crystals. Finally, the SHG relative efficiency of the sample containing Nb and Er was lower (0.7). If we compare this result with the expected one from a sample of RTP doped only with Nb and containing a similar concentration of this ion,<sup>17</sup> we can see that the SHG relative efficiency is clearly lower. This may be due to the presence of Er in the sample because this ion has a significant absorption of light from  ${}^{4}I_{15/2}$  to  ${}^{2}H_{15/2}$  manifolds in the green region.<sup>17-19</sup> We found, however, that this absorption did not dramatically decrease SHG relative efficiency, so we can conclude that the NLO properties of this crystal are as good as those of the RTP crystal.

#### **Discussion**

Figure 2 shows the structure of this family of compounds. It is a network of chains of very distorted  $TiO<sub>6</sub>$ octahedra linked by  $PO<sub>4</sub>$  octahedra with periodic bond chains of  $-PO_4-TiO_6-$  in the *a* direction and along the  $a-c$  diagonal (Figure 2a). Ti(1) and Ti(2) octahedra alternate along the *c* direction to form helicoidal chains of linked TiO<sub>6</sub> octahedra (Figure 2a,b). Each Ti(1)O<sub>6</sub> octahedron shares two corners with  $Ti(2)O_6$  octahedra through the OT(1) and OT(2) oxygens and the other four corners with  $PO<sub>4</sub>$  tetrahedra. If we take the plane containing the central Ti atom and the two OT oxygens as the equatorial plane of the Ti octahedra, then the equatorial plane of  $Ti(1)O_6$  is almost parallel to the (010) plane, the  $c$  axis is almost parallel to the  $OT(1)$ <sup>iii</sup>-OT-(2)ii (see Table 6) vector, and the *a* axis is approximately parallel to the  $OT(1)$ <sup>iii</sup>-O(1) vector. The O(5)<sup>ii</sup> and O(6)<sup>iii</sup> atoms are out of the plane and bonded to Ti(1) along a line almost parallel to the *b* axis. In the Ti(2) octahedron, the equatorial plane is almost parallel to the (100) plane and formed by O(7), O(8), OT(1), and OT(2) atoms. The  $c$  axis is approximately parallel to the  $O(8)-OT$ - $(1)$ <sup>iii</sup> vector and the apical O(3) and O(4)<sup>iv</sup> atoms are bonded to Ti(2) along a line almost parallel to the *a* axis. The typical long and short Ti-O bonds in the structure of KTP isomorphs are maintained, but if we compare their distances with those of pure RTP crystals, the Ti-  $(1)$ -OT $(1)$  and Ti $(2)$ -OT $(2)$  distances are shorter in these new crystals, while the  $Ti(1)-OT(2)$  and  $Ti(2)-$ OT(1) distances are longer (see Table 6 and ref 3). The PO4 tetrahedra are not very different from those of the





undoped RTP compounds. The  $RbO<sub>9</sub>$  cages occupy the channels left by the network of the  $TiO_6$  octahedra and PO4 tetrahedra along the *c* direction (see Figure 2c).

It is of interest to note that in this family of crystals the Ti(1)O<sub>6</sub> octahedra are larger than the Ti(2)O<sub>6</sub> octahedra. Another feature of the selective distribution of Nb is that only the former is occupied: the ionic radius of  $Nb^{5+}$  is slightly larger than the radius of  $Ti^{4+}$  $(0.64$  and  $0.605$  Å, respectively<sup>28</sup>). Taking into account the much larger radius of  $Er^{3+}$  ions (0.881 Å<sup>28</sup>), the average Ti-O bond lengths in Table 6 for  $RbTi_{0.927}$  $Nb_{0.056}Er_{0.017}OPO_4$  appear to suggest that Er has a preference for Ti(1) sites over Ti(2) sites. However, because of the importance of the errors associated to the Ti-O bond lengths in this powder sample, we cannot draw any conclusions from the differences observed.

Now we turn to the Rb vacants sites in the RTP:Nb crystal. Although EPMA measurements did not establish the stabilization of vacancies of Rb in both types of crystals, the refinement of the structures gives a clear loss of Rb in the crystals that contained only Nb. This is an interesting aspect of doping RTP with Nb: the ability of the material to self-compensate electrically for the pentavalent substitution through the loss of Rb atoms. The mean Rb-O bond length was greater in the  $Rb_{0.855}Ti_{0.955}Nb_{0.045}OPO<sub>4</sub>$  structure than in the pure RTP.<sup>4</sup> This is consistent with the expansion of the cages in the structure caused by the loss of Rb atoms. In particular, the average  $Rb(1)-O$  distance (3.000 Å) in the  $Rb_{0.855}Ti_{0.955}Nb_{0.045}OPO_4$  crystal (which has Rb vacant sites) was slightly higher than that in the  $RbTi_{0.927}Nb_{0.056}Er_{0.017}OPO_4$  and RTP crystals (2.99 and 2.994 Å, respectively). This was not observed in the Rb-  $(2)O<sub>9</sub>$  cage, which had the same average Rb $(2)$ –O bond length in all three materials: 2.993 Å (with Rb vacant sites), 2.99 Å (Nb, Er), and 2.992 Å (RTP). This indicates that when doping with pentavalent  $Nb<sup>5+</sup>$  ions, Rb vacant sites are created mainly at the Rb(1) site. This interpretation also agrees with the different occupations of the Rb(1) and Rb(2) sites refined in  $Rb_{0.855}Ti_{0.955}Nb_{0.045}$ OPO4 (see Table 3).

Although Nb enters preferentially at the Ti(1) site in both crystal structures, the Ti(1) and Ti(2) sites are very similar crystallographically. If we define the distortion parameter  $\Delta_{d} = (1/6)\sum_{n=1-6}^{6} \{ [d(Ti-0)_n - \langle d(Ti-0) \rangle ]/$  $\langle d(Ti-O)\rangle$ <sup>2</sup>, we can compare the distortion of the TiO<sub>6</sub> octahedra for our two crystals with that of other compounds of the KTP family (see Table 7). In all cases, doped and undoped, Ti(1) octahedra were more distorted than Ti(2) octahedra. Moreover, in the present concentration range, the distortion in the  $Ti(2)O_6$  octahedra of RTP was not modified by doping with Nb or co-doping with Nb and Er. In our opinion the preference for  $Nb^{5+}$ ions to occupy Ti(1) sites has an electrostatic origin rather than a steric one. If we compare the Ti-Rb bond distances in the  $Rb_{0.855}Ti_{0.955}Nb_{0.045}OPO_4$  and  $RbTi_{0.927}$  $Nb_{0.056}Er_{0.017}OPO<sub>4</sub>$  structures, we can see that these distances are quite shorter for the Ti(2) cation than for the Ti(1) cation (see Table 6). This implies that the electronic repulsion in the Ti(2) position is higher than that in the Ti(1) position. Consequently,  $Nb^{5+}$  tends to occupy Ti(1) positions to avoid this electrostatic repulsion, an interpretation that is reinforced by the very similar radius of the  $Ti^{4+}$  and  $Nb^{5+}$  ions, while in the case of  $Er^{3+}$ , because of its lower electrical charge, this effect has not been observed.

It is believed that the markedly short  $Ti(1)-OT(2)$  and  $Ti(2)-OT(1)$  bonds are partially responsible for the optical nonlinearity in this family of compounds.<sup>29</sup> Phillips et al.<sup>30</sup> showed that the lengthening of the Ti- $(1)-OT(2)$  bond to the same distance as the Ti $(1)-OT$ -(1) bond was associated with a dramatic loss in SHG. Another example is  $KSnOPO<sub>4</sub>$  (KSnP), where Ti is substituted by Sn. In this case the  $SnO<sub>6</sub>$  octahedra are practically undistorted and, interestingly, the SHG efficiency drops by a factor of 70%. Although KSnP is isostructural with KTP, its structure is much closer to that of the centrosymmetric phase *Pnan*. <sup>31</sup> In our case, by looking at the Ti-OT bonds in  $Rb_{0.855}Ti_{0.955}Nb_{0.045}$ - $OPO<sub>4</sub>$  and  $RbTi<sub>0.927</sub>Nb<sub>0.056</sub>Er<sub>0.017</sub>OPO<sub>4</sub>$ , we did not find a clear or direct relationship between the difference in these bonds and SHG efficiency (see Table 7). We are therefore led to conclude that other factors also have a great influence on nonlinearity (such as modifications in the electronic structure due to doping). Notice, finally, that chemical bond calculations made by Xue and Zhang $32-34$  for the KTP structure suggest that the K(2)- $O_9$  and  $P(2)O_4$  groups are also responsible for the nonlinear optical properties of this compound.

#### **Conclusions**

We have solved the structures of  $Rb_{0.855}Ti_{0.955}Nb_{0.045}$ OPO<sub>4</sub> and RbTi<sub>0.927</sub>Nb<sub>0.056</sub>Er<sub>0.017</sub>OPO<sub>4</sub>, two new isostructurals of KTiOPO4, and measured their SHG response. The main characteristic of these structures is that we obtained the enantiomorphic image of pure RTP. In both structures, the Nb and Er cations only went to Ti sites, and the refinements of the structures confirmed that in both materials Nb cations exclusively substituted Ti(1) sites. On the other hand, the situation for Er was undistinguishable, as it was equally distrib-

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# *Charge Self-compensation in NLO Crystals Chem. Mater., Vol. 15, No. 12, 2003* 2345

uted between Ti(1) and Ti(2) sites. We believe that this preference for Nb ions to occupy Ti(1) sites has an electrostatic origin rather than a steric one. Another remarkable feature was the ability of the material to self-compensate electrically for the pentavalent substitution through the loss of Rb atoms in the crystal that contained only Nb, but when  $Er^{3+}$  was also present, this charge self-compensation was not necessary.

Measurements of SHG relative efficiency show that both these crystals are excellent nonlinear optical materials. In RbTi<sub>0.927</sub>Nb<sub>0.056</sub>Er<sub>0.017</sub>OPO<sub>4</sub>, we observed the absorption of green light by Er, but this did not decrease SHG efficiency dramatically. Comparison of the nonlinear optical properties of these crystals with those of other members of the structural family shows

that there is no clear or direct relationship between the difference in Ti-OT bonds, or the distortion of the  $TiO_6$ octahedra, and SHG efficiency. Other factors also have a strong influence on nonlinearity.

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